

We reformulate the quantum wave equation (governing the evolution of the quantum computer's wavefunction, $|\Psi\rangle$) as a quantum Boltzmann equation (governing the occupancy probability $\langle\Psi(t)|\hat{n}_\alpha|\Psi(t)\rangle$)

- Quantum mechanical evolution equation:

$$|\Psi(t + \tau)\rangle = e^{i\hat{H}\tau/\hbar}|\Psi(t)\rangle = \hat{S}\hat{C}|\Psi(t)\rangle,$$

where \hat{S} is the streaming operator and \hat{C} is the collision operator.

- The probability of occupancy:

$$p_a(\vec{x}, t) \equiv \langle\Psi(t)|\hat{n}_\alpha|\Psi(t)\rangle,$$

where \hat{n}_α is the number operator for the α^{th} -qubit that is located at the lattice node \vec{x} and is translated along the lattice direction \hat{e}_a by action of the \hat{S} operator.

- Quantum Boltzmann equation:

$$p_a(\vec{x} + \ell\hat{e}_a, t + \tau) = p_a(\vec{x}, t) + \langle\Psi(t)|\hat{C}^\dagger\hat{n}_\alpha\hat{C} - \hat{n}_\alpha|\Psi(t)\rangle.$$

The collision matrix $\hat{C} = \bigotimes_{x=1}^V \hat{U}$, is a separable tensor product (acts on each lattice node independently) and causes local quantum entanglement of outgoing collisional configurations of the particles at each node.